Cork Institute of Technology

Higher Certificate in Engineering in Electrical Engineering-Award

(NFQ Level 6)

Autumn 2006

Electrical Engineering

(Time: 3 Hours)

Attempt Five Questions Examiners: Mr. J. Hurley

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- 1. (a) An impedance of (3-j4) Ω is connected in parallel with an impedance of (8+j6) Ω across a 20 V supply. Calculate the magnitude and power factor of the current taken from the supply. (8 marks)
 - (b) A 230 V single phase supply has the following loads: (i) incandescent lamps taking a current of 8 A at a power factor of 1.0; (ii) fluorescent lamps taking a current of 12 A at a power factor of 0.6 lagging; (iii) a motor load of 8 A at a power factor of 0.8 lagging.
 Calculate the total supply current and the power factor. (8 marks)
 - (c) What is the total power taken from the supply? (4 marks)
- 2. (a) State the numerical relationship between line and phase voltages and currents in a three-phase delta-connected load. (4 marks)
 - (b) Three coils are connected in delta to a three-phase, three wire, 400-V, 50-Hz, supply and take a line current of 10A at 0.8 power factor leading. Calculate the resistance and inductance of each coil. (10marks)
 - (c) If the coils are now connected in star across the same supply, calculate the line current and the power. (6 marks)
- 3. (a) Why is the three-phase four wire distribution normally used for A.C. distribution?(3 marks)
 - (b) A three-phase 400 V system four-wire system has the following single-phase loads:

Red phase 6 kW at 0.9 power-factor lagging,

Yellow phase 3 kW at 0.7 power factor lagging,

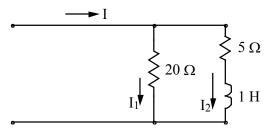
Blue phase 9 kW at 0.8 power factor lagging.

Calculate the current in each line and the neutral current.

Assume the phase sequence to be R Y B

(17 marks)

- 4. (a) Define the time-constant as applied to a circuit consisting of a resistance and an inductance connected in series. (3 marks)
 - (b) In the circuit shown the supply is 5 V D.C. and is applied to the circuit at time t = 0. Find the values of the currents I, I_1 and I_2 under final steady state conditions. Find also the time constant of the inductive branch and the value of each current after 0.1 s. (17 marks)



- 5. (a) Explain with a circuit diagram how the open-circuit test is performed on a single phase transformer. What information can be got from the open-circuit test? (5 marks)
 - (b) A single-phase transformer is rated at 1.8 kVA, 240 V/120 V. When the secondary terminals are open-circuited and the primary winding is supplied at normal voltage (240 V), the power taken is 20 W. When the secondary terminals are short-circuited, the power required to circulate full load current in the short-circuited secondary is 35 W. Calculate:

 (a) the efficiency of the transformer at full load, 0.8 power factor lagging;
 (b) the load at which maximum efficiency occurs.
- 6. (a) Explain how a rotating magnetic field is produced in a three-phase induction motor.

(5 marks)

(b) The power input to a four-pole, three-phase, 50-Hz, induction motor is 64 kW; the speed is 1470 rev/min. The stator losses are 1.2 kW and the friction and windage losses are 2.0 kW. Find (i) the slip; (ii) the output power; (iii) the rotor copper loss: (iv) the efficiency.

(15 marks)

- 7. (a) Sketch the torque speed characteristic for a series type d.c. motor. What precautions should be taken when using this type of motor? (6 marks)
 - (b) A series motor takes a current of 2 A from a 400 V d.c. supply and runs at 2,500 rev/min on light load. When the motor is loaded it takes 40 A from the same supply. Calculate the full load speed of the motor. The resistances of the armature and of the series field are 0.2 Ω and 0.1 Ω respectively. Assume that the flux is proportional to the field current and ignore the effects of armature reaction. (14 marks)

Useful Formulae

Capacitive Reactance
$$X_c = \frac{1}{\omega C} = \frac{1}{2\pi fC} = \frac{-j}{\omega C} = \frac{1}{j\omega C}$$
 (\Omega)

Inductive Reactance
$$X_L = \omega L = 2\pi f L = j\omega L$$
 (Ω)

Series Circuit

Impedance
$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$
 (\O)

$$\cos\theta = \frac{R}{Z}$$

Parallel Circuit

Two Impedances in Parallel $Z_T = \frac{Z_1 Z_2}{Z_1 + Z_2}$

Only when Z_1 and Z_2 are expressed in complex form.

Time Constant
$$T = \frac{L}{R}$$
 (s)

Growth of Current in a RL circuit

$$i = \frac{V}{R} \left\{ 1 - e^{\frac{-Rt}{L}} \right\} \tag{A}$$

Voltage across inductance
$$v_L = V \left\{ e^{\frac{-Rt}{L}} \right\}$$
 (V)

Three-Phase Star Connection

$$\begin{split} V_{Line} &= \sqrt{3} V_{Phase} \\ I_{Line} &= I_{Phase} \\ P &= \sqrt{3} V_{L} I_{L} Cos \theta \end{split} \tag{W}$$

Three-Phase Delta Connection

Power in Balanced Load

Power in Balanced Load

$$\begin{split} V_{Line} &= V_{Phase} \\ I_{Line} &= \sqrt{3} I_{Phase} \\ P &= \sqrt{3} V_{I} I_{I} Cos \theta \end{split} \tag{W}$$

Unbalanced Load
$$P_{-} = P_{-} + P_{-} + P_{-}$$
 (W)

Unbalanced Load
$$P_T = P_1 + P_2 + P_3$$
 (W)

Power Factor Correction $Cap.kVAr = kW(Tan\theta_2 - Tan\theta_1)$

Power Factor
$$= \frac{TruePower}{ApparentPower}$$

Reactive Power
$$= VISin\theta$$
 (VArs)

True Power =
$$VICos\theta$$
 (W)

Apparent Power
$$= VI$$
 (VA)

Ideal Transformer
$$\frac{V_P}{V_S} = \frac{N_P}{N_S} = \frac{I_S}{I_P}$$

Approximate Volt Drop
$$I_P \overline{R}_P Cos \theta \pm I_P \overline{X}_P Sin \theta$$
 (V)

Per Unit Regulation
$$\frac{V_{NL} - V_{FL}}{V_{NL}}$$

$$\frac{ApproximateVoltDrop}{V_{p}}x100\% \tag{\%}$$

Synchronous speed $N_s = 60 f/p$

(r/min)

(r/min)

f = frequency

p = pairs of polesPer Unit Slip $s = \frac{N_s - N_r}{N_s}$

Rotor Speed $N_r = N_s(1-s)$

Rotor Frequency $f_r = sf$

DC Machines

D.C. Motor

$$E_b = V - I_a R \tag{V}$$

$$E_{b} = V - I_{a}R$$
 (V)
$$N = K \frac{V - I_{a}R}{\phi}$$
 (r/min)
$$E_{b} = KN\phi$$

$$E_h = KN\phi$$