

Cork Institute of Technology  
Higher Certificate in Engineering in Electrical Engineering -  
Award

(NFQ Level 6)

Summer 2007

**Electrical Engineering**

(Time: 3 Hours)

Attempt **Five** Questions.

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**Q1.** (a) An impedance of  $(1.665+j10.9) \Omega$  is connected in series with two impedances of  $(12-j9) \Omega$  and  $(8+j6) \Omega$ , which are in parallel. Calculate the magnitude and power factor of the main current when the combined circuit is supplied at 30 V. Find also the voltage across each impedance.

(b) The load taken from an a.c. supply consists of: (i) a load of 30kW at 0.85 power-factor lagging; (ii) a motor load of 20kVA at 0.6 power-factor lagging; (c) a load of 15kW at 0.75 power-factor lagging.

Calculate the total load from the supply in kW and kVA and its power-factor. (7 marks)

(c) What would be the kVAr rating of a capacitor to bring the power-factor to 0.95 lagging and how would the capacitor be connected? (3 marks)

**Q2.** (a) Explain the advantage of connecting the low-voltage winding of distribution transformers in star. (5 marks)

(b) A factory has the following load with power factor of 0.85 lagging in each phase. Red phase 40 A, yellow phase 45 A and blue phase 60 A. If the supply is 400 V, three-phase, four-wire, calculate the current in the neutral and the total power. (15 marks)

- Q3. (a)** Give an expression for the time constant of a circuit consisting of a capacitor  $C$  in series with a resistor  $R$ .

A resistor is connected in series with a capacitor across a 200 V d.c. supply.

What is the voltage across the capacitor after one time constant? (5 marks)

- (b) A  $10\ \mu\text{F}$  capacitor is connected in series with a  $100\ \text{k}\Omega$  resistor across a 1000 V supply. To what voltage is the capacitor charged when the charging current has decreased to 80% of its initial value? (6 marks)
- (c) What is the time taken for the current to decrease to 40% of its initial value? (4 marks)
- (d) What is the voltage across the resistor after 3 s? (5 marks)

- Q4. (a)** With the aid of a circuit diagram show that two wattmeters can be connected to read the total power in a three-phase, three-wire system. (5 marks)

- (b) Two wattmeters connected to read the total power in a three-phase system supplying a balanced load read 25 kW and 20 kW respectively. Calculate the total power and the power factor of the load. (10 marks)
- (c) Explain the significance of: (i) equal wattmeter readings, and (ii) a zero reading on one wattmeter. (5 marks)

- Q5. (a)** Explain with a circuit diagram how the short-circuit test is performed on a single phase transformer. What information can be got from the short-circuit test? (5 marks)

- (b) A single-phase transformer is rated at 1.8 kVA, 240 V/120 V. When the secondary terminals are open-circuited and the primary winding is supplied at normal voltage (240 kV), the power taken is 18 W. When the secondary terminals are short-circuited, the power required to circulate full load current in the short-circuited secondary is 24 W. Calculate: (a) the efficiency of the transformer at full load, unity power factor; (b) the load at which maximum efficiency occurs; (c) the value of the maximum efficiency.

(15 marks)

- Q6.** (a) Describe the construction of the stator and slip ring rotor of a three-phase induction motor. Why is the motor provided with slip rings? (8 marks)
- (b) A three-phase, 50 Hz induction motor with its rotor star-connected gives 300 V at standstill between the slip rings on open circuit. Calculate the current and power factor at standstill when the rotor winding is joined to a star-connected external resistance of 8  $\Omega$  per phase. The resistance per phase of the rotor winding is 0.8  $\Omega$  and its inductance is 0.03 H. Also calculate the current and power factor when the slip rings are short-circuited and the motor is running with a slip of 3%. Assume the flux to remain constant. (15 marks)
- Q7.** (a) Explain why a starter is needed with a d.c. shunt-wound motor. Where in the circuit would the starter be connected? (5 marks)
- (b) A shunt-wound motor has a field resistance of 400  $\Omega$  and an armature resistance of 0.2  $\Omega$  and runs on a 240 V supply. The motor takes a current of 1.2 A on no-load and the no-load speed is 3500 r/min. When the motor is loaded the armature current is 32 A. Assuming that armature reaction weakens the field by 2%, calculate the speed of the motor at full load.
- (c) Give two different ways by which the speed of a shunt motor might be varied and comment on the advantages of each method. (5 marks)

## Useful Formulae

### Parallel Circuit

Two Impedances in Parallel  $Z_T = \frac{Z_1 Z_2}{Z_1 + Z_2}$

**Only when  $Z_1$  and  $Z_2$  are expressed in complex form.**

### Transients in RC-Networks

Time Constant  $T = RC$  (s)

Charging

Growth of voltage across a capacitor

$$v_c = V \left\{ 1 - e^{-\frac{t}{RC}} \right\} \quad (\text{V})$$

$$i = \frac{V}{R} e^{-\frac{t}{RC}} \quad (\text{A})$$

Discharging

$$v_c = V \left\{ e^{-\frac{t}{RC}} \right\} \quad (\text{V})$$

$$i = \frac{V}{R} e^{-\frac{t}{RC}} \quad (\text{A})$$

### Three-Phase

Unbalanced Load  $P_T = P_1 + P_2 + P_3$  (W)

Power Factor Correction  $Cap.kVAr = kW(Tan\theta_2 - Tan\theta_1)$

$$\text{Power Factor} = \frac{\text{TruePower}}{\text{ApparentPower}}$$

Reactive Power =  $VI\sin\theta$  (VAr)

True Power =  $VI\cos\theta$  (W)

Apparent Power =  $VI$  (VA)

## Two Wattmeter Method

$$\text{Total Power} \quad W_1 + W_2 \quad (\text{W})$$

$$\tan \theta = \sqrt{3} \frac{W_1 - W_2}{W_1 + W_2}$$

## The Transformer

$$\frac{\text{Output Power}}{\text{Output Power} + \text{Iron Losses} + \text{Copper Losses}} \times 100\%$$

## The Three-Phase Induction Motor

$$\text{Synchronous speed } N_s = 60f/p \quad (\text{r/min})$$

f = frequency

p = pairs of poles

$$\text{Per Unit Slip } s = \frac{N_s - N_r}{N_s}$$

$$\text{Rotor Speed } N_r = N_s(1 - s) \quad (\text{r/min})$$

$$\text{Rotor Frequency } f_r = sf$$

$$\text{Rotor EMF per phase at standstill } E_r \quad (\text{V})$$

$$\text{Rotor Reactance per phase at standstill } X \quad (\Omega)$$

$$\text{Rotor Current per phase at standstill } I_r = \frac{E_r}{\sqrt{R^2 + X^2}} \quad (\text{A})$$

$$\text{Rotor Power Factor at standstill } \cos \theta = \frac{R}{\sqrt{R^2 + X^2}}$$

At Slip s

$$\text{Rotor EMF per phase at slip s } sE_r \quad (\text{V})$$

$$\text{Rotor Reactance per phase at slip s } sX \quad (\Omega)$$

$$\text{Rotor Current per phase } \frac{sE_r}{\sqrt{R^2 + (sX)^2}} \quad (\text{A})$$

$$\text{Rotor Power Factor } \frac{R}{\sqrt{R^2 + (sX)^2}}$$

## DC Machines

### D.C. Motor

$$E_b = V - I_a R \quad (\text{V})$$

$$N = K \frac{V - I_a R}{\phi} \quad (\text{r/min})$$

$$E_b = KN\phi$$